

1. Find $\frac{dy}{dx}$ implicit differentiation, if $y^3 + 3xy = x^5$.

$$\begin{aligned} \frac{d}{dx} (y^3 + 3xy) &= \frac{d}{dx} (x^5) \\ \frac{d}{dx} (y^3) + \frac{d}{dx} (3xy) &= \frac{d}{dx} (x^5) \\ 3y^2 \cdot \frac{dy}{dx} + \left(3x \cdot \frac{d}{dx} y + y \cdot \frac{d}{dx} 3x \right) &= 5x^4 \\ 3x^2 + \left(3x \cdot \frac{dy}{dx} + y \cdot 3 \right) &= 5x^4 \\ 3y^2 \frac{dy}{dx} + 3x \frac{dy}{dx} + 3y &= 5x^4 \\ (3y^2 + 3x) \frac{dy}{dx} &= 5x^4 - 3y \\ \frac{dy}{dx} &= \frac{5x^4 - 3y}{3y^2 + 3x} \end{aligned}$$

2. Find $\frac{dy}{dx}$ implicit differentiation, if $\sin(x^2y) = 2x$.

$$\begin{aligned} \frac{d}{dx} (\sin(x^2y)) &= \frac{d}{dx} (2x) \\ \cos(x^2y) \cdot \frac{d}{dx} (x^2y) &= 2 \\ \cos(x^2y) \cdot \left(x^2 \frac{d}{dx} y + y \frac{d}{dx} x^2 \right) &= 2 \\ \cos(x^2y) \cdot \left(x^2 \frac{dy}{dx} + 2xy \right) &= 2 \\ x^2 \cos(x^2y) \frac{dy}{dx} + 2xy \cos(x^2y) &= 2 \\ x^2 \cos(x^2y) \frac{dy}{dx} &= 2 - 2xy \cos(x^2y) \\ \frac{dy}{dx} &= \frac{2 - 2xy \cos(x^2y)}{x^2 \cos(x^2y)} \end{aligned}$$